

$$2.7 \quad 1 - P(A) - P(B) + P(A \cap B) = (a + b + c + d) - (a + b) - (a + c) + a = d = P(A' \cap B')$$

$$2.8 \quad P[(A \cap B') \cup (A' \cap B)] = b + c = (a + b) + a + c - 2a = P(A) + P(B) - 2P(A \cap B) \quad \text{Refer to Figure 2.6}$$

$$2.9 \quad (a) \quad P(A) + P(B) - P(A \cap B) \geq 0 \rightarrow P(A \cap B) \leq P(A) + P(B)$$

$$(b) \quad P(A) + P(B) - P(A \cap B) \leq 1 \quad P(A \cap B) \geq P(A) + P(B) - 1$$

$$2.15 \quad \frac{p}{1-p} = \frac{A}{B}, \quad pb = A - Ap, \quad PA + pB = A, \quad p(A+B) = A, \quad p = \frac{A}{A+B}$$

$$2.17 \quad (a) \quad P(A|B) = \frac{P(A \cap B)}{P(B)} \geq 0; \quad (b) \quad P(B|B) = \frac{P(B \cap B)}{P(B)} = \frac{P(B)}{P(B)} = 1$$

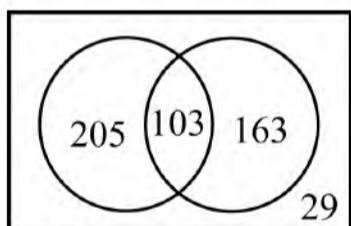
$$(c) \quad P(A_1 \cup A_2 \cup \dots | B) = \frac{P[(A_1 \cup A_2 \cup \dots) \cap B]}{P(B)} \\ = \frac{P(A_1 \cap B)}{P(B)} + \frac{P(A_2 \cap B)}{P(B)} + \dots \\ = P(A_1|B) + P(A_2|B) + \dots$$

- 2.39 (a) House has fewer than three baths;
 (b) does not have fire place;
 (c) does not cost more than \$200,000
 (d) is not new;
 (e) has three or more baths and fire place;
 (f) has three more baths and costs more than \$200,000
 (g) costs more than \$200,000 but has no fire place;
 (h) is new or costs more than \$200,000
 (i) is new or costs \$200,000 or less
 (j) has 3 or more baths and/or fire place;
 (k) has 3 or more baths and/or costs more than \$200,000;
 (l) is new and costs more than \$200,000

$$2.43 \quad 3, x_1 3, x_1 x_2 3, x_1 x_2 x_3 3, \dots \text{ where } x_i = 1, 2, 4, 5, 6, \text{ for all } i$$

$$(a) \quad 5^{k-1}; \quad (b) \quad 1 + 5 + \dots + 5^k = \frac{5^{k+1} - 1}{4}$$

$$2.50 \quad 500 - (308 + 266) + 103 = 29 \neq 59 \text{ results are inconsistent}$$



- 2.54 (a) $1 - 0.37 = 0.63$; (b) $1 - 0.44 = 0.56$; (c) $0.37 + 0.44 = 0.81$;
 (d) 0; (e) 0.37, $P(A \cap B') = P(A)$ for mutually exclusive events;
 (f) $1 - 0.81 = 0.19$

- 2.55 (a) Probability cannot be negative.
 (b) $0.77 + 0.08 = 0.85 \neq 0.95$
 (c) $0.12 + 0.25 + 0.36 + 0.14 + 0.09 + 0.07 = 1.03 > 1$
 (d) $0.08 + 0.21 + 0.29 + 0.40 = 0.98 < 1$

$$2.60 \quad \frac{\binom{16}{2}}{\binom{52}{2}} = \frac{120}{1326} = \frac{20}{221}$$

$$2.63 \quad (a) \quad \frac{\binom{6}{2} \binom{5}{2} \binom{3}{2} \cdot 4}{6^5} = \frac{15 \cdot 10 \cdot 3 \cdot 4}{6 \cdot 6 \cdot 6 \cdot 6 \cdot 6} = \frac{25}{108}$$

$$(b) \quad \frac{6 \binom{5}{3} \cdot 5 \cdot 4}{6^5} = \frac{6 \cdot 10 \cdot 5 \cdot 4}{6 \cdot 6 \cdot 6 \cdot 6 \cdot 6} = \frac{25 \cdot 4}{648} = \frac{25}{162}$$

$$(c) \quad \frac{6 \cdot 5 \binom{5}{3} \binom{2}{2}}{6^5} = \frac{6 \cdot 5 \cdot 10}{6 \cdot 6 \cdot 6 \cdot 6 \cdot 6} = \frac{25}{648}$$

$$(d) \quad \frac{6 \binom{5}{4} \cdot 5}{6^5} = \frac{6 \cdot 5 \cdot 5}{6 \cdot 6 \cdot 6 \cdot 6 \cdot 6} = \frac{25}{1296}$$